"As for everything else, so for mathematical theory: beauty can be perceived but not explained."

Arthur Cayley

- 1. Draw the following intervals on the number line.
  - (a) [-1,4) (c)  $(3,\infty)$
  - (b) (2,6) (d)  $(-\infty,5]$
- 2. Write as an interval:  $\{x : x \in \mathbb{R}\}$ ; i.e., "The set of all x, where x is a real number." Draw this interval on the number line.
- 3. Plot on the number line:  $[-2,3) \cap \mathbb{Z}$ ; i.e., "The intersection of [-2,3) with the set of integers."
- 4. Arrange from least to greatest:  $|-\pi|$ , |-3|, 3, -|-4|, -4. Use the symbols "<" and " $\leq$ ".
- 5. Simplify to an integer:  $|2(|-1-3| \cdot |6-8|) 5|$
- 6. Rewrite |x+2| |1-x| without using the absolute value sign, where:
  - (a) x < -2
  - (b)  $x \ge 4$
  - (c) x = 0
- 7. Write using the absolute value sign the expression representing the distance on the number line between 3 and -1.
- 8. Write using the absolute value sign: "The distance between x and -2 is greater than or equal to 3."
- 9. Consider the intervals [-4, 3] and [1, 8).
  - (a) Draw these intervals on the number line and mark the interval representing their intersection.
  - (b) Express the intersection in interval notation.
  - (c) Express the intersection in set notation without using the absolute value sign.
  - (d) Express the intersection using the absolute value sign.
- 10. Write as a union of two intervals:  $\{x : |x-3| > 4\}$ .
- 11. Plot on the number line:  $\{x : |x+2| \le 5\}$
- 12. Plot on the number line:  $\{x : |4 x| \ge 1\}$
- 13. Solve and write the answer in set notation: -2 < x 3 < 4.
- 14. Solve and write the answer in interval notation:  $|x+4| \leq 5$  and x > -3.
- 15. Solve and write the answer using absolute value: -7 < 1 x < -5.