

1. Find the leading term and use it to determine the long-term behavior of each polynomial function.

(a) $f(x) = x^3 + 2x - 1$ x^3 , $f(x) \rightarrow \infty$ as $x \rightarrow \infty$, $f(x) \rightarrow -\infty$ as $x \rightarrow -\infty$

(b) $f(x) = -x^2 + 4$ $-x^2$, $f(x) \rightarrow -\infty$ as $x \rightarrow \pm\infty$

(c) $f(x) = -(x+2)^2(x-1)(x-3)^2$ $-x^5$, $f(x) \rightarrow -\infty$ as $x \rightarrow \infty$, $f(x) \rightarrow \infty$ as $x \rightarrow -\infty$

(d) $f(x) = (x^2 + 2x - 1)^2(3x - 5)^4$ $81x^8$, $f(x) \rightarrow \infty$ as $x \rightarrow \pm\infty$

2. Find all roots and their degrees. Describe the behavior of the graph at each root.

(a) $g(x) = (x+1)(x-2)^2(x-4)$ $x = -1$, deg 1, $x = 2$, deg 2, $x = 4$ deg 1

(b) $g(x) = (2x-1)(x+6)^4$ $x = \frac{1}{2}$, deg 1, $x = -6$, deg 4

(c) $g(x) = (x^2 - 5x + 6)(x^2 - 16)$ $x = 3$, deg 1, $x = 2$, deg 1, $x = 4$ deg 1, $x = -4$ deg 1

(d) $g(x) = (x^2 + 1)(x^2 - 9)^2$ $x = -3$, deg 2, $x = 3$, deg 2

3. Give the degree of each polynomial function. At most how many turning points does each graph have?

(a) $h(x) = x(x+7)(x-2)(x-5)$ Degree 4. At most 3 turning points

(b) $h(x) = (x-5)^2(x+3)^3$ Degree 5. At most 4 turning points

(c) $h(x) = (x^3 + 2x - 1)^2$ Degree 6. At most 5 turning points

(d) $h(x) = x^2(3x+4)^2(x^2-3x+1)^3$ Degree 10. At most 9 turning points

4. Sketch the graph of each polynomial function. Label all roots with their degrees and mark all intercepts. The graph must be smooth and continuous.

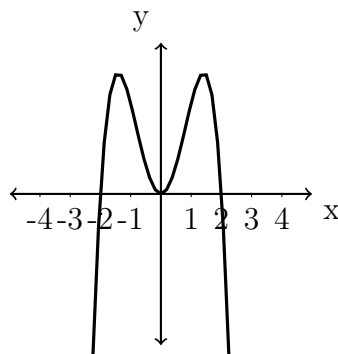
(a) $f(x) = x(x-1)(x-3)(x-5)$

(c) $f(x) = (x^2 + 4x + 3)^2$

(b) $f(x) = -(x-2)^2(x+1)^3$

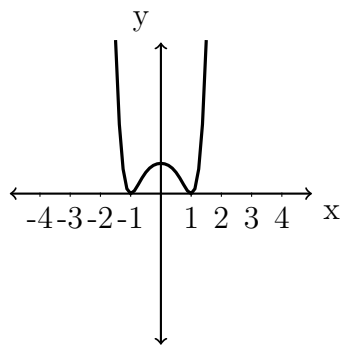
(d) $f(x) = (x-1)^2(x^2 + 4x + 4)(3-x)$

5. *Working backwards.* Find a possible polynomial function for each graph with the given degree. The y -axis is left intentionally without scale.



(a) degree 4

Possible solution: $f(x) = -x^2(x+2)(x-2)$



(b) degree 6

Possible solution: $f(x) = (x + 1)^4(x - 1)^2$