

1. Perform polynomial division.

$$(a) \frac{x^3 + 2x^2 - 3x - 6}{x + 2} x^2 - 3$$

$$(b) \frac{x^5 + x^3 + 3x^2 - 4}{x^2 + 1} x^3 + 2x + 3 + \frac{2x-1}{x^2-1}$$

$$(c) \frac{x^3 - 2x^2 + 4x + 1}{x - 3} x^2 + x + 7 + \frac{22}{x-3}$$

2. What is the remainder when you divide the following polynomial by $x + 1$?

$$(a) p(x) = 2x^3 + 3x^2 + x + 8 \quad -14$$

$$(b) p(x) = x^4 + x^3 + x - 2 \quad -5$$

$$(c) p(x) = x^3 + 4x^2 + 2x - 1 \quad -8$$

3. When does a the graph of a quadratic equation open upward, and when does it open downward? (Hint: Leading Coefficient) **When the leading coefficient is positive the graph opens upward, when the leading coefficient is negative the graph opens downward.**

4. For the following quadratic equations find (i) the vertex, (ii) the x-intercepts (how many are there?), (iii) the y-intercepts, and (iv) sketch the graph.

$$(a) f(x) = x^2 - 3x + 8$$

$$i. \left(\frac{3}{2}, \frac{23}{4}\right)$$

$$ii. \text{None, discriminant} < 0$$

$$iii. (0, 8)$$

$$(b) f(x) = 2x^2 - 4x - 1$$

$$i. (1, -3)$$

$$ii. 2 \text{ x-intercepts, } x = 1 \pm \frac{\sqrt{6}}{2}$$

$$iii. (0, -1)$$

$$(c) f(x) = x^2 + 2x - 3$$

$$i. (-1, -4)$$

$$ii. 2 \text{ x-intercepts, } x = 1, x = -3$$

$$iii. (0, -3)$$

5. What are the shifts and reflections needed to obtain these graphs from a basic function? State the basic function in each scenario and sketch the graph of $g(x)$.

$$(a) g(x) = (x - 3)^2 + 1 f(x) = x^2, \text{ shift right 3 units, up 1 unit}$$

$$(b) g(x) = -x^3 + 1 f(x) = x^3, \text{ reflect across the } x \text{ axis (or } y \text{) and shift up 1}$$

$$(c) g(x) = -\frac{1}{(x-1)^2} f(x) = \frac{1}{x^2}, \text{ reflect across the } x \text{ axis, and right 1 unit.}$$

$$(d) g(x) = \sqrt{x} + 2 f(x) = \sqrt{x}, \text{ shift up 2 units}$$