

1. Put the following lines in slope-intercept form, and find two points on the line.

(a) $3x - 7y = 12$
 $y = 12 + \frac{3}{7}x$, possible points $(0, \frac{12}{7}), (1, \frac{15}{7})$

(b) $\frac{1}{5}y + x - 10 = 0$
 $y = 50 - 5x$, $(0, 50), (10, 0)$

(c) $\frac{2}{3}x + \frac{1}{3}y = 2$
 $y = 6 - 2x$, $(0, 6), (1, 4)$

2. Find a line parallel to $y = 3x + 4$ passing through the origin.

$$y = 3x$$

3. Find a line perpendicular to $y - 4 = 3(x + 1)$ that passes through the point $(2, 2)$.

$$y = -\frac{1}{3}x + \frac{7}{3}$$

4. Put the following expressions in set notation using absolute value signs.

(a) $-2 < x < 0$
 $\{x : |x + 1| < 1\}$

(b) $-7 < x + 3 < 3$
 $\{x : |x + 3| < 5\}$

(c) $3 \leq x - 2 \leq 9$
 $\{x : |x - 8| < 3\}$

5. Solve by factoring.

(a) $x^2 - 2x - 3$
 $(x - 3)(x + 1) \Rightarrow x = 3, -1$

(b) $2x^2 + 7x - 4$
 $(2x - 1)(x + 4) \Rightarrow x = \frac{1}{2}, -4$

(c) $10x^2 - 11x - 6$
 $(5x + 2)(2x - 3) \Rightarrow x = \frac{3}{2}, -\frac{2}{5}$

6. Solve the following rational expressions.

(a) $\frac{1}{x} = \frac{2x-4}{x-1}$
 $x = \frac{5 \pm \sqrt{17}}{4}$

(b) $\frac{3x}{2} = \frac{3x+1}{x-1}$
 $x = \frac{9 \pm \sqrt{105}}{6}$

(c) $\frac{x+2}{5} - \frac{x}{x-4} = 0$
 $\{8, -1\}$

7. Solve using key number method.

$$(a) \frac{(x+1)x}{x+4} \leq 0$$
$$(-\infty, -4) \cup [-1, 0]$$

$$(b) \frac{(x+2)^2}{(x-3)} > 0$$
$$(3, \infty)$$

$$(c) \frac{(x-3)(x+3)}{2x} \geq 0$$
$$(-\infty, -3) \cup (0, 3)$$

8. Solve by completing the square

$$(a) x^2 + 8x + 7 = 0$$
$$\{1, 7\}$$

$$(b) 2x^2 - 12x + 12 = 0$$
$$3\{\pm\sqrt{3}\}$$

9. Find the center and radius of the circle.

$$(a) x^2 + y^2 - x + 2y - 5 = 0$$
$$\text{Center: } \left(-\frac{1}{2}, -1\right), r = \frac{5}{2}$$

$$(b) x^2 + y^2 - 4x - 8y = 0$$
$$\text{Center: } (2, 4), r = \sqrt{20}$$

10. Simplify.

$$(a) \frac{(xy)^6}{(x^{-2}y^{-4})^{-1}}$$
$$x^4y^2$$

$$(b) (xy^2)^2 - (x^{-1})^{-2}$$
$$x^2(y^4 - 1)$$

$$(c) \left(\frac{(x^{\frac{1}{2}}y^3)^{\frac{1}{3}}}{(xy)}\right)^{\frac{3}{2}}$$
$$\frac{1}{x^{\frac{5}{4}}}$$

$$(d) (\sqrt{4} + 32^{\frac{1}{5}})^2$$
$$16$$

11. Rationalize the denominator and simplify.

$$(a) \frac{1}{\sqrt{x-2}}$$
$$\frac{\sqrt{x+2}}{x-4}$$

$$(b) \frac{\frac{2x}{x+\sqrt{3}}}{\frac{2x(x-\sqrt{3})}{x^2-3}}$$

$$(c) \frac{\frac{2}{x^{\frac{3}{4}}}}{\frac{2x^{\frac{1}{4}}}{x}}$$

$$(d) \frac{\frac{4}{\sqrt{x-3}+2}}{\frac{4\sqrt{x-3}-8}{x+1}}$$

12. Let $f(x) = x^3 - 2$ and $g(x) = x - 1$. Compute the following. (No need to simplify for e,f)

$$(a) (f + g)(0) = -3$$

$$(b) (fg)(a) = a^4 - a^3 - 2a + 2$$

$$(c) \frac{f(x+h)-f(x)}{h} = \frac{(x+h)^3 - x^3}{h}$$

This is as far as you need to go since its Cubed. If squared I expect you to simplify as much as possible.

$$(d) \frac{g(x+h)-g(x)}{h} = 1$$

$$(e) (f \circ g)(x) = (x-1)^3 - 2$$

$$(f) (f \circ g)^{-1}(x) = \sqrt[3]{x+2} + 1$$

13. Find the inverse of each function (if possible), and the domain and range of both f and f^{-1} . (If there is no inverse find the domain of the function.)

$$(a) f(x) = 3x - 4$$

$$f^{-1}(x) = \frac{1}{3}x + \frac{4}{3}, \text{ Domain} = \text{Range} = (-\infty, \infty)$$

$$(b) f(x) = \sqrt[3]{x} + 2$$

$$f^{-1}(x) = (x-2)^3, \text{ Domain} = \text{Range} = (-\infty, \infty)$$

$$(c) f(x) = \frac{1}{x-5}$$

$$f^{-1}(x) = \frac{1}{x} + 5 \text{ Domain (of } f) = (-\infty, 5) \cup (5, \infty)$$

$$(d) f(x) = (x+2)^2$$

Inverse function only exists on restricted domain of $[0, \infty)$, where the Range is $[0, \infty)$. Inverse is $f^{-1}(x) = \sqrt{x} - 2$