

## Probability: Binomial Probability

1. For  $n$  repeated trials, with constant probability of success  $p$  for all trials, find the probability of exactly  $x$  successes.

(a)  $n = 5, p = \frac{1}{3}, x = 4$   ${}_5C_4 \left(\frac{1}{3}\right)^4 \left(\frac{2}{3}\right) = \frac{10}{3^5}$

(b)  $n = 10, p = .9, x = 6$   ${}_{10}C_6 (.9)^6 (.4)^4 = \frac{9^7}{10^9}$

(c)  $n = 20, p = \frac{1}{8}, x = 5$   ${}_{20}C_5 \left(\frac{1}{8}\right)^5 \left(\frac{7}{8}\right)^{15} =$

(d)  $n = 10, p = .3, x = 2$   ${}_{10}C_2 (.3)^2 (.7)^8 =$

2. Manny has a .320 batting average, meaning he hits the ball with success rate  $p = .32$ . In a game against a rival team he will bat 10 times. Find the probability he will get more than two hits in the series.  $1 - {}_{10}C_2 (.32)^2 (.68)^8 - {}_{10}C_1 (.32) (.68)^9 - (.68)^{10}$

3. Benji Roberts is taking a ten question multiple choice test of which each question has three answer choices, only one of which is correct. Benji decides on answers by rolling a fair die and marking the first answer choice if he rolls a 1 or 4, the second if he rolls a 2 or 5, and the third if he rolls a 3 or 6. Find the probability of the following events.

(a) He marks exactly 3 correct answers.  $.2601$

(b) He marks less than 3 correct answers.  $.2991$

(c) He marks atleast 7 correct answers

(d) He marks 10 correct answers.  $\frac{1}{3^{10}}$

4. During a presidential campaign, 58% of the political columns in a group of major newspapers were favorable to the incumbent president. If a sample of 10 of these columns is selected at random, what is the probability that none of them will be favorable to the incumbent president?  $.0001708$